One-page Teacher Guide

- 1. Assess to find point-of-need first: Use the Fluency Interview (downloadable for free from www.toptenresources.com/fluency) to work out at which skill each student should begin from at the start of the year (before you start whole-class). Each year, pass this data along (using the whole-school tracker spreadsheet) to avoid needing to repeat the entire interview, and simply commence it at the next question.
- 2. 5 minute morning/afternoon routine only: This is a <u>5-minute daily routine</u> (ideally the first routine of the morning, or a final routine of the afternoon before students go home) separate to the main hands-on maths lesson each day.

Note: Ideally, the main maths lesson every day is a real-life linked, hands-on, materials-based task involving understanding, reasoning and problem-solving (not procedural, algorithmic or speed/fluency focused). Our hands-on, sequential numeracy units (free samples at https://www.toptenresources.com/earlyyears and https://www.toptenresources.com/years3-6) have been developed for over a decade in Australian classrooms by numeracy coaches to support teachers with the huge task of planning these types of tasks.

Fluency is not worth any more than 5 minutes of students' time per day, and students should not be working on a sheet for more than 5 minutes per day.

- 3. **15 in 5:** When a student completes 15 problems (the entire sheet) for three days in a row within the 5-minute timeframe (therefore averaging 20 seconds or less per problem), they are considered fluent in that skill and can progress to the next skill.
- 4. Write and wipe: We recommend using write-and-wipe boards to reduce printing and teacher workload.
- 5. Immediate feedback for students with peer correction using a calculator: Students can swap and correct with calculators for *Skill 21* onwards. If some students are not up to Skill 21 yet, organise swaps for peer correction amongst students who are up to that skill and beyond, or students can correct their own work with a calculator and teacher 'glance-check' afterwards.

Pull a domino and add both sides. Use what you know about all the ways to make 3, 4, 5, 6, 7, 8 and 9 from ninja number sliders.

PB:

Skip-count by 10 and 5 from zero.

Skip-count by 10

Skip-count by 5

0	0	5
10	10	

Skip-count by 2 from zero.

Skip-count by 2:

	T	T	Г	
0	2	4		
L	1	1	1	

Roll a 20-sided die and work out one less.

Think one back

Roll a 20-sided die and work out two less.

Think two back

Roll two 10-sided dice to make a two-digit number, then work out one more.

Think one more

Roll two 10-sided dice to make a two-digit number, then work out two more.

Think two more

+ 2 =	+ 2 =
+ 2 =	+ 2 =
two more =	two more =
two more =	two more =
two more =	two more =
two greater =	two greater
two greater =	PR:

Roll two 10-sided dice to make a two-digit number, then work out one less.

Think one back

- / =	- / =
- / =	– / =
one back =	one back =
one less =	one less =
one less =	one less =
one fewer =	one fewer =
one fewer =	PB:

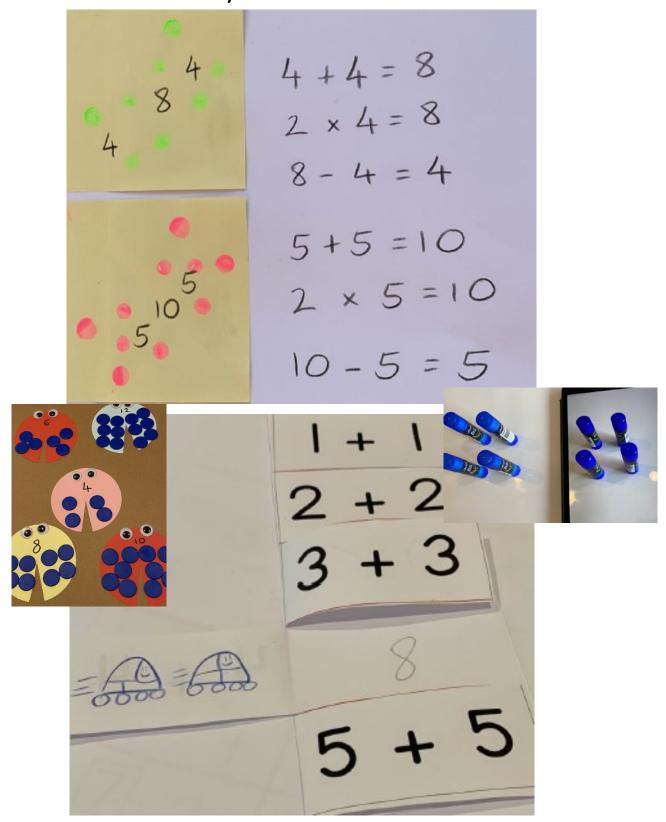
Roll two 10-sided dice to make a two-digit number, then work out two less.

Think two back

- 2 =	- 2 =
- 2 =	- 2 =
two back =	two back =
two less =	two less =
two less =	two less =
two fewer =	two fewer =
two fewer =	PB:

Initial support for the doubles strategy, using doubles dot paintings, doubles flipbooks, mirrors or iPad photos to double objects, ladybirds and much more!

See Early Years Addition Unit 6



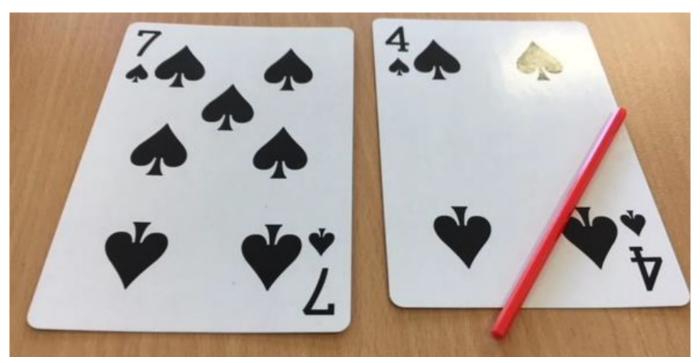
Roll a 10-sided die and double the number.

Roll a 10-sided die, write down that number. Then write a number that is one less/more than it. Work out the addition.

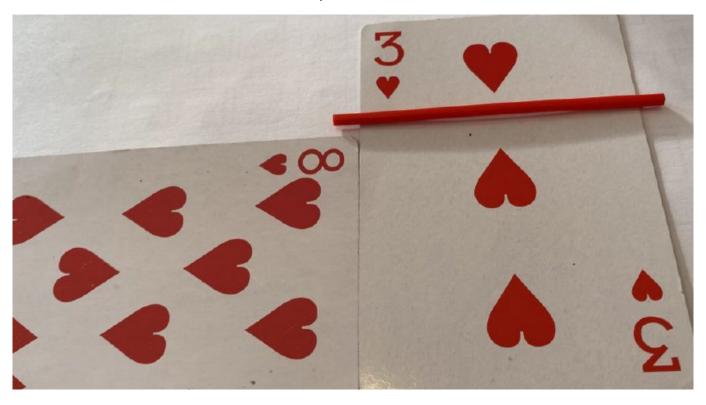
Double and one or two more/less. one less than one more than number rolled number rolled + +one less than one more than number rolled number rolled +one less than one more than number rolled ++two more than two less than number rolled number rolled ++two less than two more than number rolled number rolled two more than two less than +two more than number rolled + PR:

Initial support for the build/bridge to 10 strategy using a partitioning stick on the playing cards, like so:

Use the stick to 'mark' a ten, then add the rest.



"7 and 3 is 10, and 1 more is 11."



"8 and 2 is 10, and 1 more is 11."

Create one side of a deck of cards with 7-9, and another side with 3-5. Remove 1, 2, 10 and all picture cards. Keep sides separate, turn over one from each pile and add together.

PB:

Addition strategy codes

$$10 f = 10 fact$$

bt10 = build/bridge to 10

Addition strategy codes

$$10f = 10 fact$$

bt10 = build/bridge to 10

Addition strategy codes

$$10 f = 10 fact$$

bt10 = build/bridge to 10

Pull two playing cards (1-10, remove picture cards) and add them together.

Think about all the ways to make/ninja sliders. 10 facts. doubles. near doubles and build to 10.

Code your strategy (n = ninja ways to make 10f = 10 fact d = double nd = near double bt10 = build to 10)

+ =

+ =

+ =

+ =

+ =

+ =

+ =

+ =

+ =

+ =

+ =

=

+ =

+ =

+

PB:

Use a deck of cards (remove 10 and picture cards). Pull two cards to <u>make a two-digit number</u>. Add ten to that number.

Think one ten more (the ones don't change).

Use a deck of cards (remove 10 and picture cards). Pull two cards to make a two-digit number. Subtract ten from that number.

Think one ten less (the ones don't change).

Use a deck of cards (remove 10 and picture cards). Pull two cards to <u>make a two-digit number</u>. Add 2 tens to that number.

Think two tens more (the ones don't change).

PB:

Use a deck of cards (remove 10 and picture cards). Pull two cards to make a two-digit number. Subtract 2 tens from that number.

Think two tens less (the ones don't change).

Roll two tens dice (place value dice that show tens such as 10, 20, 30, up to 90). Add the two tens numbers together.

Connect this to all the strategies and facts you know for single-digit addition.

+	=		+] =
J			J	ן



Roll two tens dice (place value dice that show tens such as 10, 20, 30, up to 90). Keep the larger number on the left. Work out the difference.

Connect this to all the strategies and facts you know for single-digit subtraction.

	J	
_	=	_ =
	=	_ =
_	=	_ =
	_ =	=
		=
		=
		=
	 =	PB:

Roll one 20-sided die. Double the number and write the total.

Think about doubling the tens, then the ones, then putting that together.

Addition strategy codes

$$10f = 10 fact$$

Addition strategy codes

$$10f = 10 fact$$

Addition strategy codes

$$10f = 10 fact$$

Roll two 20-sided dice. Add using your addition strategies (ways to make ninjas, 10 facts, doubles, near doubles, build to 10).

Code your strategies (nd = near double bt10 = build to 10)

Roll two 20-sided dice. Subtract the smaller from the larger using mental strategies. Keep the larger number on the left side.

Think about reversing the addition strategies you know.

_	Ξ	_ =
_	Ξ	_ =
_	Ξ	_ =
_	Ξ	_ =
_	Ξ	_ =
_	Ξ	_ =
_	Ξ	_ =
_	=	PB:

Pull two cards from a deck (remove 10 and all picture cards) to <u>make a two-digit number</u>. Double the number and write the total.

Think about doubling the tens, then the ones, then putting that together.

Pull 4 playing cards (remove 10 and picture cards) to make two 2-digit numbers. <u>Estimate</u> the total roughly (<u>do not answer</u>).

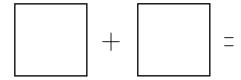
Estimation needs to be quick and rounded (not exact answers).

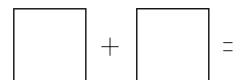
+	\approx	$+$ \approx
+	\approx	$+$ \approx
+	\approx	$\boxed{} + \boxed{} \approx$
+	\approx	$+$ \approx
+	\approx	PB:

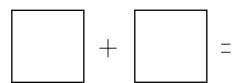
Pull 4 playing cards (remove 10 and picture cards) to make two 2-digit numbers. Add mentally (not vertically).

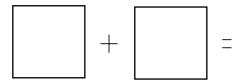
Think split strategy, jump strategy and switch strategy.

	_	_
		_









PB:

Pull 4 playing cards (remove 10 and picture cards) to make two 2-digit numbers. Keep the larger number is on the left.

Estimate the difference roughly (do not answer).

Estimation needs to be quick and rounded (not exact answers).

$oxed{-}$	$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$
lacksquare	$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$
lacksquare	$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$
lacksquare	$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$
lacksquare	$\boxed{} = \boxed{} \approx$
lacksquare	$\boxed{} = \boxed{} \approx$
$\boxed{} \sim \boxed{} \approx$	$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$
\sim	PB:

Pull 4 playing cards (remove 10 and picture cards) to make two 2-digit numbers. Keep the larger number is on the left.

Work out the difference mentally (not vertically).

Think jump back, jump the gap, transformation (pump it up or drop it low) mental strategies.

_	=		_		=	<u>-</u>
_	=					_
_	=					
_	=					
_	=					
_	=					
-] -	_ 			1	PB:	

Skip-count by 4 from zero.

0	4	8	

Skip-count by 3 from zero.

0	3	6				

Pull two playing cards (10 and picture cards removed) to make three different two-digit starting numbers.

extra challenge option: Create a three-digit starting number.

starting number	Skip-count c	on by 9 (think	add 10, ta	ke away 1):
different				
starting number	Skip-count c	on by 8 (think	add 10, ta	ke away 2):
different starting number	Skip-count c	on by 7 (think	add 10, ta	ke away 3):

Multiplicative Strategies

strategy codes

Doubling family

x2 think double d 2 x 8 = think double 8 = 16

x4 think double double 4 x 7 = think double double 7 double 7 is 14, double 14 is 28

d7 = 14, dd = 28

x8 think double double

ddd

8 x 6 = think double double double double 6 is 12, double double is 24, double double double = 48

Tens family

x10 think place value pattern (one place value higher) pv

5 x 10 = 50 because it is now 5 tens instead of 5 ones, as it increases in size by 10

x9 think x10 - group, check digits = 9 pv - g

 $9 \times 7 = \text{think 7 tens is 70, take away 7 to make it 9 sevens instead of 10 sevens so <math>70 - 7 = 63$, check that '6' and '3' is 9 - correct!

x5 think x10 half pv 1/2

5 x 6 = think 6 tens halved, so 60 halved is 30

Threes

x3 think double + group d+g

3 x 6 = think double 6 + one more 6, so 12 + 6 = 18

x7

You only need to memorise 7x7=49 and you have all the other strategies already!

x6 think x3 double it, or 5x + group x3d

6 x 7 = think x3, so 3 x 7 = 21, double it to make it 6x7, so 42

Pull a card from a deck (remove all picture cards). Multiply that number by 4.

Think double double (dd)

Pull a card from a deck (remove picture cards). Multiply by 3.

Think double plus a group (d + g)

Pull a card from a deck (remove picture cards). Multiply by 10.

Think in **tens** ($4 \times 10 = 4$ tens = 40) and that each digit shifts higher by one place value (pv)

Pull a card from a deck (remove picture cards). Multiply by 5.

Think in **tens** then halve it to make it fives $(pv^{\frac{1}{2}})$

Pull a card from a deck (remove picture cards). Multiply by 9.

Think in **tens** then take away one group (pv - g)

Pull a card from a deck (remove all picture cards). Multiply by 8.

Think double double (ddd)

Pull a card from a deck (remove picture cards). Multiply by 6.

Think $\times 3$ double it, or $\times 5$ + group, or d + d + d

Pull a card from a deck (remove picture cards). Multiply by 7.

Use all multiplicative strategies so far so you only need to learn 7 × 7

Pull two cards from the deck (remove picture cards). Multiply together using all multiplicative strategies.

Think back to all multiplicative strategies

			_	
groups of	=		×	Ξ
groups of	=		×	Ξ
groups of	=		×	Ξ
groups of	=		×	Ξ
groups of	=		×	Ξ
groups of	=		×	Ξ
groups of	=		×	Ξ
groups of	=	PB:		

Pull cards to fill the first row and first column of this grid (remove picture cards). Multiply the numbers together. Fill the grid with the answers within 5 minutes.

×					

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Score out of	100.	100	0	/c

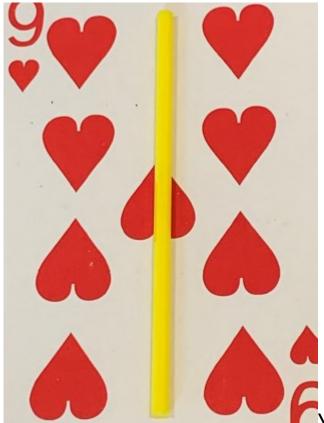
Roll a 10-sided die and a 20-sided die. Multiply together using all multiplicative strategies.

Think back to all multiplicative strategies

groups of	=		×	=
groups of	=		×	Ξ
groups of	=		×	=
groups of	=		×	Ξ
groups of	=		×	Ξ
groups of	=		×	=
groups of	=		×	Ξ
groups of	=	PB:		

Initial practice:

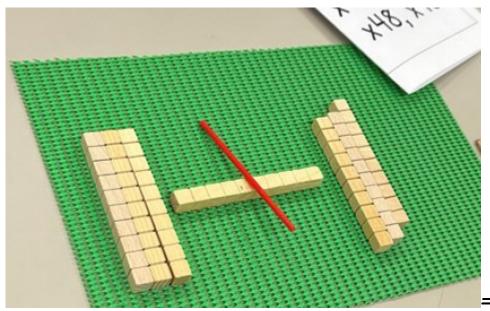
Halve the numbers on the playing cards using partitioning sticks:



You can see 4 and a half on each side.

Initial practice:

For example, for halving 70, split the tens between two sides (60 becomes 30 and 30). For the extra ten, split it into 5 and 5.



= 35

Pull a card from a deck (remove all picture cards). Halve that number.

Think the opposite of doubling. For odd numbers think half of the even number one less than it, then halve the extra one.

$$\frac{1}{2} \sigma f =$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$
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$$\frac{1}{2} \sigma f$$

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$$\frac{1}{2} \sigma f$$
 =

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$
 =

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

Roll a tens place value die (die that shows 10, 20, 30 up to 90). Halve that number.

Think the opposite of doubling. What and what makes that number? For numbers like 90 think half of 80, then half of the extra ten.

$$\frac{1}{2} \sigma f =$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$
 =

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$
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$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$
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$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$

$$\frac{1}{2} \sigma f$$
 =

Pull two cards from a deck (remove 10 and all picture cards) to <u>form a two-digit number</u>. Halve that number to divide/share it between 2.

Think half to divide by 2 (share between 2)

$$\frac{1}{2} \sigma f =$$

$$\frac{1}{2} \sigma f =$$

Post-it note cups for the following skills

Create post-it note cups (a cup filled with post-it notes or the labels below scrunched up) that contain all the multiples of that family. This ensures students can divide without remainders during the following skills, using the inverse of the multiplicative strategy or multiplication fact family.

Slice, scrunch up and fill a cup with these for dividing by 4:

4	8	1 2	16
2 0	24	28	3 2
3 6	40	80	100

Slice, scrunch up and fill a cup with these for dividing by 8:

8	16	24	3 2
40	48	5 6	64
7 2	80	160	200

Slice, scrunch up and fill a cup with these for dividing by 10:

10	20	3 0	40
50	60	7 0	80
90	100	200	1000

Slice, scrunch up and fill a cup with these for dividing by 5:

5	10	15	20
2 5	3 0	3 5	40
45	<i>5</i> O	100	1000

Slice, scrunch up and fill a cup with these for dividing by 3:

3	6	9	1 2
1 5	18	2 /	24
2 7	3 0	300	900

Slice, scrunch up and fill a cup with these for dividing by 6:

6	1 2	18	24
3 0	3 6	42	48
54	60	600	1200

Slice, scrunch up and fill a cup with these for dividing by 9:

9	18	2 7	3 6
45	<i>5</i> 4	6 3	7 2
8 /	90	180	900

Slice, scrunch up and fill a cup with these for dividing by 7:

7	14	2 /	2 8
3 5	42	49	5 6
6 3	7 0	140	700

Create a post-it note cup with scrunched up notes that show a multiple of 4. Pull a post-it note from the cup and divide it by 4.

Halve it and halve it again (half of half)

$$\frac{1}{4} \sigma f = \div 4$$

$$\frac{1}{4} \sigma f$$
 = $\div 4$

Create a post-it note cup with scrunched up notes that show a multiple of 8. Pull a post-it note from the cup and divide it by 8.

Halve it, halve it, and halve it again (half half)

$$\frac{1}{8} \sigma f =$$

$$\frac{1}{8} \sigma f =$$

Create a post-it note cup with scrunched up notes that show a multiple of 10. Pull a post-it note from the cup and divide it by 10.

Think one place value less

Create a post-it note cup with scrunched up notes that show a multiple of 5. Pull a post-it note from the cup and divide it by 5.

Divide by 10 (shifts one place value less) then double it

$$\frac{1}{5} \sigma f$$
 = $\div 5$

$$\frac{1}{5} \sigma f$$
 = $\div 5$ =

Create a post-it note cup with scrunched up notes that show a multiple of 3. Pull a post-it note from the cup and divide it by 3.

$$\frac{1}{3} \sigma f =$$

$$\frac{1}{3} \sigma f =$$

Create a post-it note cup with scrunched up notes that show a multiple of 6. Pull a post-it note from the cup and divide it by 6.

$$\frac{1}{6} \sigma f$$
 = $\div 6$

$$\frac{1}{6} \sigma f$$
 = $\div 6 =$

Create a post-it note cup with scrunched up notes that show a multiple of 9. Pull a post-it note from the cup and divide it by 9.

$$\frac{1}{9} \sigma f$$
 = $\div 9 =$

$$\frac{1}{9} \sigma f = \div 9$$

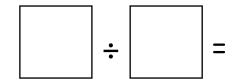
Create a post-it note cup with scrunched up notes that show a multiple of 7. Pull a post-it note from the cup and divide it by 7.

$$\frac{1}{7} \sigma f$$
 = $\div 7$

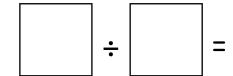
$$\frac{1}{7} \sigma f$$
 = $\div 7$

Pull two playing cards (remove 10 and picture cards) to form a two-digit number. Roll a 10-sided die to divide it by the rolled number.

Use the multiplication fact family and adjust for remainders

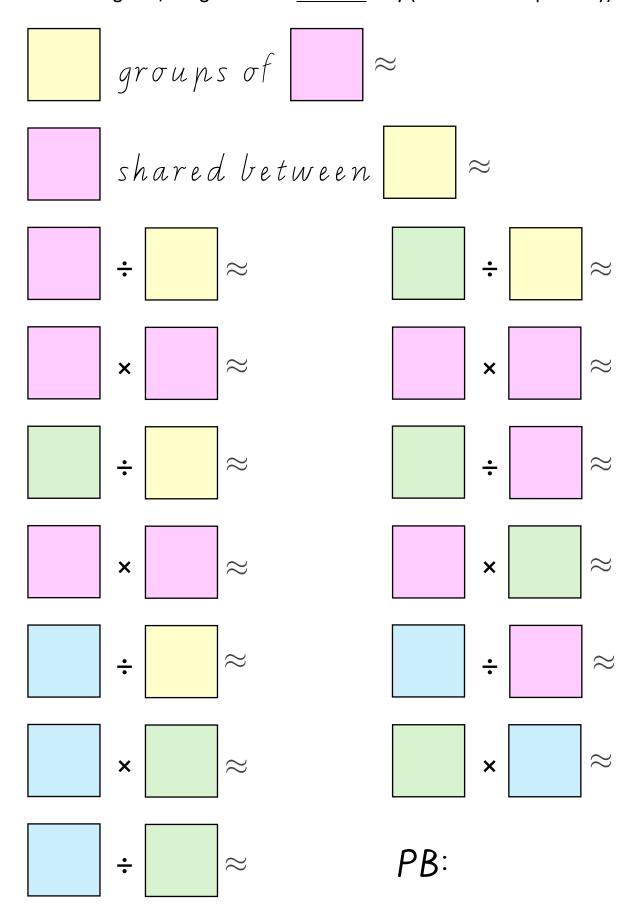


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Pull cards (remove 10 and picture cards) to fill the blanks with 1-digit numbers for yellow boxes, 2-digit numbers for pink boxes, 3-digit numbers for green, 4-digit for blue. Estimate only (do not answer precisely).



Pull cards (remove 10 and picture cards) to fill the blanks.

Multiplying by powers of 10 shifts the place values higher. Dividing by powers of 10 shifts the place values lower.

Pull two cards from a deck (remove 10 and picture cards) to <u>form a two-digit number</u>. Work out 50% of that number.

extra challenge option: three-digit number.

Think half (share between 2).

$$\frac{1}{2} \sigma f$$
 =

$$\frac{1}{2} \sigma f$$
 =

$$\frac{1}{2} \sigma f$$
 =

$$\frac{1}{2}$$
 \times =

÷ 2 =

Pull two cards from a deck (remove 10 and picture cards) to <u>form a two-digit number</u>. Work out 25% of that number.

extra challenge option: three-digit number.

Think share between 4 (half of half).

$$\frac{1}{4} \sigma f$$

$$\frac{1}{4} \sigma f$$

$$\frac{1}{4} \sigma f$$

Pull two cards from a deck (remove 10 and picture cards) to <u>form a two-digit number</u>. Work out 10% of that number.

extra challenge option: three-digit number.

Think power of 10 place value shift.

$$\frac{1}{10} \sigma f$$
 =

$$\frac{1}{10} \sigma f$$

$$\frac{1}{10} \sigma f$$